Interpretability and Causal Inference for Global Time Series Forecasting Methods

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Overview

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- 3 Local Interpretable Model Agnostic Rule-based Explanations for Forecasting (LIMREF)
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- Priscila Grecov (Causal Inference)

Local Vs Global Time Series Forecasting

Local Models	Global Models
Build one forecasting model per each series	Build one forecasting model across many series
Fit local parameters separately on each series	Fit global parameters that are the same across many series
Amount of parameters is small per series, but grows with amount of series	Amount of parameters stays the same
Models need to be simple, as not much data	Models can be more complex
Examples: SES, Theta, ETS, ARIMA, Prophet, TBATS	Examples: ES-RNN, DeepAR, NBEATS,

For a given time-series a global model is typically more complex and less interpretable than a local model

Causal Inference

Accuracy vs Interpretability in Machine Learning

Trade-off between accuracy and interpretability

General Solution in Machine Learning: Post-hoc Local Model-Agnostic Interpretability



Causal Inference

Local Interpretability For Classification

- We want an explanation for one particular instance
- Assumption: The behaviour of the instance to be explained is similar to the behaviour of the instances in its neighbourhood



- Select a neighbourhood
- Sample new instances from the neighbourhood (change the features)
- Run your global model on the sampled instances to get the labels
- Train an interpretable model on the neighbourhood plus generated labels, to mimic the global model in the neighbourhood of the instance

Our goal

Transfer the concept of local interpretability as closely as possible to global time-series forecasting models:

- The global forecasting model is seen as a black-box model, the framework should be model-agnostic
- We want (local) explanations for one particular time series out of a big set of series
- Our neighbourhood is a particular series (could also use more series chosen with a similarity like DTW)
- Problems:
 - How to sample from the neighbourhood?
 - How to run the global model on the samples?
 - Which local explainer to use?
 - How to train the local explainers on the output of the global model in the neighbourhood?

Proposed Solution

How to sample from the neighbourhood? / How to run the global model on the samples?

 No sampling, only actual instances from the neighbourhood: Use the fit of the global model to the particular time series.



Proposed Solution Cont.

- Using the in-sample fit of the global model without sampling may seem like a bad idea, especially if the global model overfits.
- But: Finding of Montero-Manso and Hyndman (2021):

The in-sample error of the global model is usually higher than the local model while it generalizes better

Bootstrapping:

- Generate new time series using bootstrapping, by bootstrapping the remainder of STL decomposition from the original series using a Moving Block Bootstrap (MBB) technique
- Bootstrap the remainder of the fit of the time series using MBB

Proposed Solution Cont.

- We assume that local statistical methods are interpretable, though this can be disputed.
- The goal of our work is to make global models as interpretable as local models.

Which local explainer to use?

- ETS
- TBATS
- MSTL & STL
- Prophet
- DHR-Arima
- Theta

Decompositions (trend, seasonality, remainder)

Proposed Methodology



Example 1

San Francisco Traffic Hourly Dataset

TBATS interpretation: Forecasts plot



Example 1 Cont.

TBATS interpretation: Decomposition plot



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Example 2

Ausgrid Half-hourly Dataset

Prophet interpretation: Forecasts plot



Example 2 Cont.

Prophet interpretation: Decomposition plot



Example 3: Bootstrapped Models

Kaggle Web Traffic Dataset

ETS interpretation: Forecasts plot



Example 3 Cont.

ETS interpretation: Chosen Model Summary Plot



How to Evaluate Local Explainers?

- **Comprehensibility:** How interpretable are the explanations?
- Fidelity: How well does the explanation approximate the forecast of the global model?
- Consistency: How consistent are the explanations of the explainer across multiple runs?
- Accuracy: How well does an explainer forecast unseen data?

Fidelity_Actual

Error can be sMAPE, MASE, RMSE, or MAE

Fidelity_Actual = Error(global,explainer) - Error(global,actual)

- **Fidelity_Actual** < 0, the global model is closer to the explainer model than the actual.
- Fidelity_Actual > 0, the global model is closer to the actuals than the explainer model.

Fidelity_Local

Fidelity_Local= Error(global,explainer) - Error(global,local)

- Verifies whether the local explainer is closer to the global model forecasts than the local model to the global model forecasts.
- **Fidelity_Local** < **0**, explainer model is closer to the global model.
- **Fidelity**_**Local** > **0**, local model is closer to the global model.

Fidelity_with_Explainer

Fidelity_with_Explainer = Error(global,explainer) - Error(local,explainer)

- Verify whether the local explainer is closer to the global model than the local model.
- **Fidelity_with_Explainer** < **0**, the explainer model is closer to the global model
- **Fidelity_with_Explainer** > **0**, the explainer model is closer to the local model

Accuracy Explainer & Local model

Explainer & Local model = Error(actual,explainer) - Error(actual,local)

- Verify whether the local explainer performs better than the local model.
- **Explainer & Local model** < **0**, the explainer model performs better than the local model
- **Explainer & Local model** > **0**, local model performs better than the local explainer.

Accuracy Explainer & Global model

Explainer & Global model = Error(actual,explainer) - Error(actual,global)

- Verify whether the local explainer performs better than the global model.
- **Explainer & Global model** < **0**, the explainer model performs better than the global model
- Explainer & Global model > 0, global model performs better than the local explainer

Accuracy Global and Local Model

Global and Local Model = Error(actual,global) - Error(actual,local)

- Verify whether the global model performs better than the local model.
- Global and Local Model < 0, the global model performs better than the local model
- Global and Local Model > 0, local model performs better than the global model

Experiments Results

Table 1: Mean SMAPE measures of the datasets for different local explainer models

Dataset	Local	Fidelity_Actual	Fidelity_Local	Explainer and	Explainer and	Fidelity_with	Global and
	Explainer			Local Model	Global Model	Explainer	Local Model
nn5_weekly	es	-0.082	-0.066	-0.008	0.006	-0.072	-0.013
	prophet	-0.050	-0.024	-0.000	0.003	-0.011	-0.004
	dhr_arima	-0.058	-0.021	-0.003	0.000	-0.011	-0.003
	tbats	-0.069	-0.036	-0.022	0.006	-0.022	-0.028
ausgrid_weekly	es	-0.074	-0.043	-0.024	0.019	-0.001	-0.043
	prophet	-0.063	-0.020	-0.015	0.018	0.067	-0.033
	dhr_arima	-0.082	-0.030	-0.015	0.009	0.038	-0.024
	tbats	-0.089	-0.022	-0.007	0.021	0.009	-0.028
	stl	-0.076	-0.039	-0.026	0.015	0.014	-0.041
kaggle_web_traffic_daily	ets	-0.401	-0.210	-0.074	0.003	-0.196	-0.077
	theta	-0.404	-0.164	-0.047	0.003	-0.151	-0.049
sf_traffic_hourly	tbats	-0.017	-0.020	-0.006	0.000	-0.018	-0.006
	prophet	-0.011	-0.016	-0.013	0.008	-0.009	-0.021
	dhr_arima	-0.013	-0.025	-0.014	0.000	-0.013	-0.014
	mstl	0.000	-0.015	-0.006	0.010	-0.008	-0.016
ausgrid_half_hourly	tbats	-0.149	-0.197	-0.119	0.000	-0.168	-0.119
	prophet	-0.070	-0.237	-0.167	0.054	-0.207	-0.221
	dhr_arima	-0.110	-0.121	-0.063	0.016	-0.019	-0.079
	mstl	0.034	-0.160	-0.108	0.131	-0.180	-0.239

Conclusions: LoMEF

- General trade-off between accuracy and interpretability
- Global Forecasting Models typically more complex than Local Models
- Translate Local Model Agnostic Post-Hoc interpretability to Global Forecasting Models
 - Neighbourhood fit of the global model on original or bootstrapped series
 - Local interpretable models Statistical models
- Goal: Focus on interpretability, not predictive accuracy
- Proposed local explainer performed models performed well in terms of Accuracy, Fidelity, and Consistency
- With this model, global models can be made as interpretable as local models

Local Interpretable Model Agnostic Rule-based Explanations for Forecasting (LIMREF)

Introduction

- The method was developed for the "FUZZ-IEEE Competition on Explainable Energy Prediction", where it was the winning method
- Competition: Forecast the monthly electricity consumption for 3248 households in a coming year
 - Half-hourly energy consumption data during for 1 year period
 - Prediction horizon 12 months

Goal

Provide accurate and explainable forecasts for one year period

Proposed Methodology

Accurate Predictions

Introduced an energy prediction framework using global models to generate accurate forecasts

Explaining Predictions

Introduced a novel algorithm to produce local rule-based explanations for global time-series forecasting

Methodogy: How to Generate Accurate Predictions

- Our model is based on the model that achieved 4th place in a past competition on the same data
 - Uses daily series to trade-off granularity and complexity
 - Learns across series (global models), which is state of the art in forecasting -CIF2016, M4, M5 Competitions

Exogenous Variables

- Calendar effects
- Temperature Uses bootstrapping to generate future temperatures



Methodology: Proposed Solution

LoRMIkA ? \longrightarrow Time-series forecasting

Proposed novel local model-agnostic interpretability approach to explain the forecast produced by global time-series models and produce Rule-based explanations

Proposed framework will keep the global forecasting model as a black-box model, in a model-agnostic way











Table 2: Original Values of the Instance to be Explained

Mean Consumption	Max Consumption	Min Consumption	Temperature	Month	Monthly Forecast
3.5708kWh	6.131kWh	0kWh	5.98C	February	129.27kWh

Current Supporting Rules

(What are the current conditions that support the global model prediction?)

Your predicted consumption is 129.27kWh. Because you are in month February.

Table 3: Original Values of the Instance to be Explained

Mean Consumption	Max Consumption	Min Consumption	Temperature	Month	Monthly Forecast
3.5708kWh	6.131kWh	0kWh	5.98C	February	129.27kWh

Current Contradicting Rules

(What are the current conditions that contradict the global model prediction?)

The conditions that currently exist that indicate a risk of an increased consumption by 118.85kWh for the particular month are 5.82 < average temperature \leq 6.20 & month = February & minimum consumption \leq 0.00.

Table 4: Original Values of the Instance to be Explained

Mean Consumption	Max Consumption	Min Consumption	Temperature	Month	Monthly Forecast
3.5708kWh	6.131kWh	0kWh	5.98C	February	129.27kWh

Hypothetical Supporting Rules

(What are the hypothetical conditions that support the global model prediction?)

The conditions that need to be satisfied to maintain the monthly predicted consumption would be 6.01 < average temperature ≤ 6.31 .

Table 5: Original Values of the Instance to be Explained

Mean Consumption	Max Consumption	Min Consumption	Temperature	Month	Monthly Forecast
3.5708kWh	6.131kWh	0kWh	5.98C	February	129.27kWh

Hypothetical Contradicting Rules

 (What are the hypothetical conditions that could potentially invert the global model prediction? Counterfactual Rules)

If you have mean consumption > 9.16 it will increase your consumption by 275.53kWh.

A Complete Explanation of LIMREF

Table 6: Original Values of the Instance to be Explained

Mean Consumption	Max Consumption	Min Consumption	Temperature	Month	Monthly Forecast
3.463kWh	6.973kWh	0kWh	6.308C	February	119.01kWh

Your predicted consumption is 119.02kWh. Because you have month=February. If you have mean consumption > 13.99 it will increase your consumption by 388.48kWh. The conditions that currently exist that indicate a risk of an increased consumption by 179.55kWh for the particular month are 6.05 < average temperature ≤ 6.31 & month=February & min consumption ≤ 0.00 . The conditions that need to be satisfied to maintain the monthly predicted consumption would be average temperature > 6.31. Please note that here the mean, min and max consumption is calculated over the last 20 days. The temperature is the average temperature throughout the predicted month.

Conclusions: LIMREF

- Provide accurate and self-explaining predictions of the future monthly electricity consumption in a coming year
 - Accurate predictions Train a global model (Expectile Regression)
 - Interpretable predictions Proposed a novel explainability algorithm
- Explanations
 - Simple rules
 - Complete rules

Causal Inference Using Global Forecasting Models for Counterfactual Prediction

ARTIFICIAL COUNTERFACTUAL

IDEA: to forecast an artificial **counterfactual trend** for the units affected by intervention (**treated units**) based on a large-dimensional panel of observed time-series from a pool of untreated peers (**control units**)





HOW TO MEASURE

THE ACCURACY

OF A

COUNTERFACTUAL?

PLACEBO TESTS:

1. NULL EFFECT of the treatment for the control units: errors of the control group (= effect of the intervention over the controls) must be very low



2. SIGNIFICANT DIFFERENCE between the errors from treated and control units (error gaps must be statistically significantly different from each other)





AUSTRALIAN EMS CALLS

79 time series

Training period: 41 points

Forecasting period: 12 points

Intervention: Effect of the increase of number liquor licenses over the EMS calls demand

911 EMERGENCY CALLS

62 time series 7 Training period: 41 points Forecasting period: 7 points 10 intervention: Effect of the COVID-19 lockdown over 911 calls demand



Table 1. Results for the 79 monthly series of NASS.

Aethod	Mean sMAPE	Median sMAPE	Mean MASE	Median MASE
DeepCPNet-ALI				
All LGAs	0.1396	0.1341	0.9786	0.9467
Treated Group	0.1405	0.1341	0.9812	0.9413
Control Group	0.1332	0.1357	0.9604	0.9733
STM-univariate				
All LGAs	0.1557	0.1537	1.0828	1.0205
Treated Group	0.1570	0.1560	$_{-1.0900}$	1.0205
Control Group	0.1464	0.1323	1.0331	0.9716
ARIMA		•		•
All LGAs	0.1560	0.1458	1.0888	0.9853
Treated Group	0.1572	0.1427	$_{-1.0973}$	0.9643
Control Group	0.1476	0.1490	1.0300	1.0069
TS		-		•
All LGAs	0.1507	0.1441	1.0647	1.0078
Treated Group	0.1515	0.1427	1.0705	0.9981
Control Group	0.1450	0.1555	1.0244	1.0876

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OUR EXPERIMENTS

AUSTRALIAN EMS CALLS

79 time series Training period: 41 points Forecasting period: 12 points Intervention: Effect of the increase of number liquor licenses over the EMS calls demand

911 EMERGENCY CALLS

62 time series

Training period: 41 points

Forecasting period: 7 points

Intervention: Effect of the COVID-19 lockdown over 911 calls demand





Table 2. Results for the 62 monthly series of 911 emergency calls.

		METHODS								
	(Control Group					Treated Group			
Error Metric	DeepCPNet	\mathbf{LS}	STM-uni	ARIMA	ETS	DeepCPNet	LSTM-uni	ARIMA	ETS	
Mean sMAPE	0.1899		0.1945	0.1847	0.1920	0.2525	0.2525	0.2508	0.2624	
Median sMAPE	0.1740	L	0.1783	0.1717	0.1746	0.2290	0.2256	0.2250	0.2336	
Mean MASE	0.8521	L	0.8698	0.8288	0.8616	1.3939	1.3926	1.3857	1.4498	
Median MASE	0.9176		0.9370	0.9272	0.9430	1.3100	1.2842	1.2848	1.3334	

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OUR EXPERIMENTS – Simulated datasets Monte Carlo experiment

S.1) Linear DGP: ARIMA + Var(3,4)

a. Exogenous Variable (regressor) = RGCE (with four lags) using a stationary LINEAR ARIMA DGP to build 100 time-series

S.2) Non-linear DGP: SETAR + Var(3,4)

a. Exogenous Variable (regressor) = RGCE (with four lags) using NONLINEAR SETAR DGP to build 100 time-series

100 time-series

- b. Endogenous Variables on VAR(3,4) multivariate DGP process + inclusion of 1 regressor (RGCE):
 - RCPI --> within NN modelling will enter as exogenous
 - RGDPG --> within NN modelling will enter as exogenous
 - UNRATE --> within NN modelling will enter as endogenous

5

70 control

30 treated



VAR(3,4) DGP for endogenous and SETAR DGP for exogenous

Average unrate by control and treated group - DGP: VAR(3,4) for endog (with) and SETAR for exog

DeepCPNet-adam vs. DeepCPNet-EX-adam - considering predictor as exogenous variable



RESULTS for Simulated Data – simulation 2 using non-linear DGP:

DeepCPNet achieves the best results in the scenario with non-linear relationships across the time series



Control Units Prediction Errors

Counterfactual Prediction Errors



Model	meanSMAPE	medianSMAPE	Model	meanSMAPE	medianSMAPE
DeepCPNet	0.03457	0.03833	DeepCPNet	0.03578	0.03351
DeepCPNet_EX	0.01406	0.01227	DeepCPNet_EX	0.00672	0.00799
Arima	0.05706	0.06374	Arima	0.06597	0.07375
VAR4	0.01771	0.01582	VAR4	0.05156	0.06027
CausalImpact	0.02478	0.02260	CausalImpact	0.00684	0.00663
SCM	0.02832	0.03066	SCM	0.03515	0.02812

Idea: What about Probabilistic Forecasting?

Study of target interventions affecting only the tails or the variance of the treated units' distribution rather than their mean or median (i.e., interventions affecting only parts of the distribution)

Inspection of the impacts of interventions over skewed or heavytailed distributions

It allows for decision-making under uncertainty by precisely predicting intervals to quantify forecast uncertainties



OUR NOVELTY PROBABILISTIC GFM COUNTERFACTUAL and CAUSAL EFFECT distribution predictions

DeepProbCP:

SOLUTION: global + Recurrent NN + probabilistic forecasting and inference framework to perform counterfactual distributional predictions



SIMULATION DESIGN OF THE INTERVENTION OVER TREATED UNITS





- Treated units: 50 units (randomly chosen)
- length = 220 observations

Intervention:

- how: adding a constant of 1.574 (= 1 standard deviation from the treated units before the intervention) for the values > quantile 90%
- The intervention causes:
 - + 1.5% in the median + 4.3% in the mean > + 25% left tail

STEPS OF **DeepProbCP**:

Step 1) DeepCPNet (GFM-RNN-LSTM based stacked model):

 the MAE error function is replaced by the "pinball loss" (quantile loss) during the training and hyperparameter tuning processes

 $L_{\tau}(y,\hat{y}) = \tau(y-\hat{y})_{+} + (1-\tau)(\hat{y}-y)_{+}$

• estimate the future trajectory for each control and treated time series post-intervention, based on their (and covariates) preintervention data:

$$\{y_{j,T_0+1:T}\}_{j=1}^J = m_G(y_{j,1:T_0}, \mathbf{x}_{j,1:T_0}, \Theta)$$

where $m_G(\cdot)$ is a multi-layer RNN with LSTM cells under the stacked design:

$$\mathbf{h}_{j,t} = r(\mathbf{h}_{j,t-1}, y_{j,t-1}, \mathbf{x}_{j,1:T_0}, \Theta)$$

$$where: = \begin{bmatrix} \tau \dots \text{ some quantile} & J \dots \text{ each time series} \\ y \dots \text{ observed data} & T_0 \dots \text{ intervention time} \\ \hat{y} \dots \text{ forecast data} & \Theta \dots \text{ set of parameters} \\ (\cdot)_{+} = \max(0, \cdot) & h_t \dots \text{ hidden states} \end{bmatrix}$$

Step 2) The step 1 is performed for each chosen quantile:

$$\begin{cases} (\hat{y}_{t+1,:j}^{(\tau_1)}, ..., \hat{y}_{t+k,:j}^{(\tau_k)}) &= m_G(h_t, x_{:t,j}^{(h)}, \tau_1) \\ (\hat{y}_{t+1,:j}^{(\tau_2)}, ..., \hat{y}_{t+k,:j}^{(\tau_2)}) &= m_G(h_t, x_{:t,j}^{(h)}, \tau_2) \\ \cdots \\ (\hat{y}_{t+1,:j}^{(\tau_Q)}, ..., \hat{y}_{t+k,:j}^{(\tau_Q)}) &= m_G(h_t, x_{:t,j}^{(h)}, \tau_Q) \end{cases}$$

Step 3) Each forecasted quantile from step 2 is used to build the quantile distribution

- using cubic splines functions, we interpolate each one the forecasted quantiles to build the "Quantile Distribution Function".
- we also estimate the quantile distribution function by splines for the observed data post-intervention



- 1) Simulated Data:
 - a. Simulated intervention



b. Estimated quantile distributions using splines

Treated units:





Results of the **EXPERIMENTS (1)**

Simulated Data*: 1)

Placebo Tests C



* 51 control time series and 50 treated time series using the nonlinear DGP emploving SETAR models

d. Performance comparing with benchmark models

POINT METRIC ERROR RESULTS FOR THE 101 SIMULATED SERIES GENERATED BY SETAR

		Mean	Median	Mean	Median
	Method	sMAPE	sMAPE	MASE	MASE
	DeepProbCP-0.50				
Error gaps	- Treated Group	0.2088	0.1770	1.2202	0.9420
estimation for	- Control Group	0.1892	0.1407	1.0322	0.8665
future	CausalImpact				
trajectory:	- Treated Group	0.3237	0.2915	1.8509	1.6781
	- Control Group	0.3561	0.3016	1.9302	1.8983
	ArCo				
	- Treated Group	0.2834	0.2488	1.6575	1.3993
	- Control Group	0.2494	0.2206	1.3851	1.0676

Causal Effect Prediction Errors

errors

with the

recovered

effect:





2) Real-world data – Australian EMS calls:



b. Estimated quantile distributions using splines

Treated units:



Conclusions

- Global RNN-based approaches (combination of global modelling, stacked architecture, LSTM cells, and COCOB optimizer) should emerge as a new generation of machine learning models in the causal inference task of predicting counterfactual outcomes, not being restricted to the pure forecasting tasks.
- The powerful causal inference mechanism developed in this research can contribute to leverage the estimation of causal effect's measurement which is crucial to guide and support the policymakers: (i) in their decision making processes, and (ii) evaluation of their policies





Conclusions Cont.

With this **causality-inspired DNN model** combined with **non-parametric probabilistic techniques** we can:

- improve the generalisation and adaptivity of the framework by leveraging the causality analysis to achieve reliable causal effect identifications in realworld scenarios.
- enrich the decision-making process with powerful tools capable of not only delivering point predictions of counterfactuals but also predictions of their distributions.





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Thank you!

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